

# Advanced Techniques for Mobile Robotics

## SLAM Front-Ends

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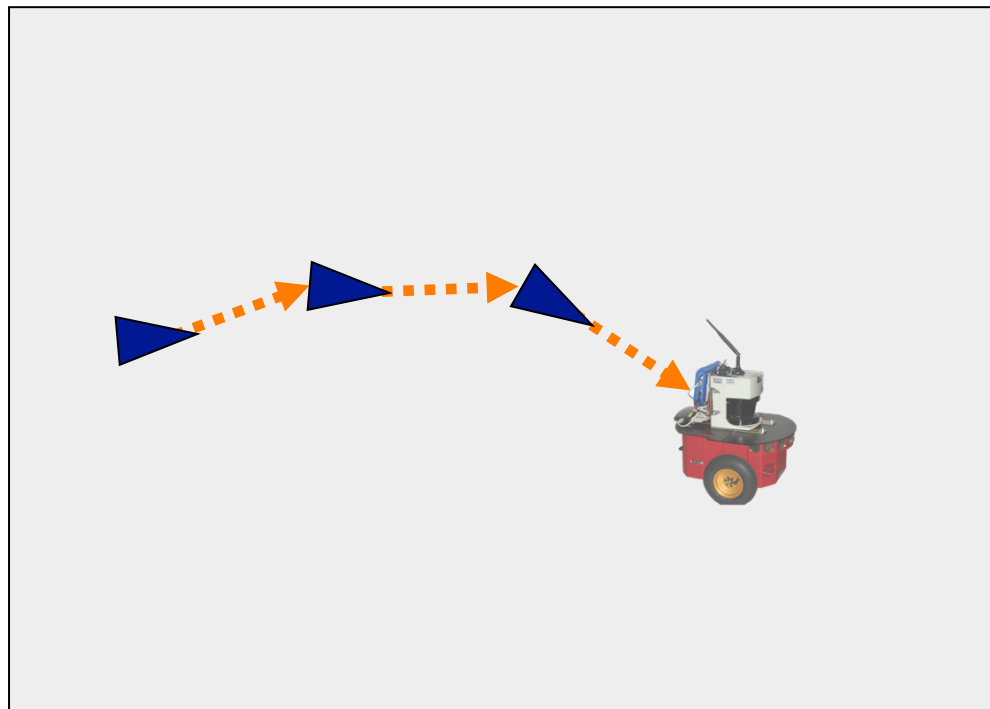
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Partial image/slide courtesy by Edwin Olson

# SLAM

- Constraints connect the poses of the robot while it is moving via odometry

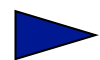
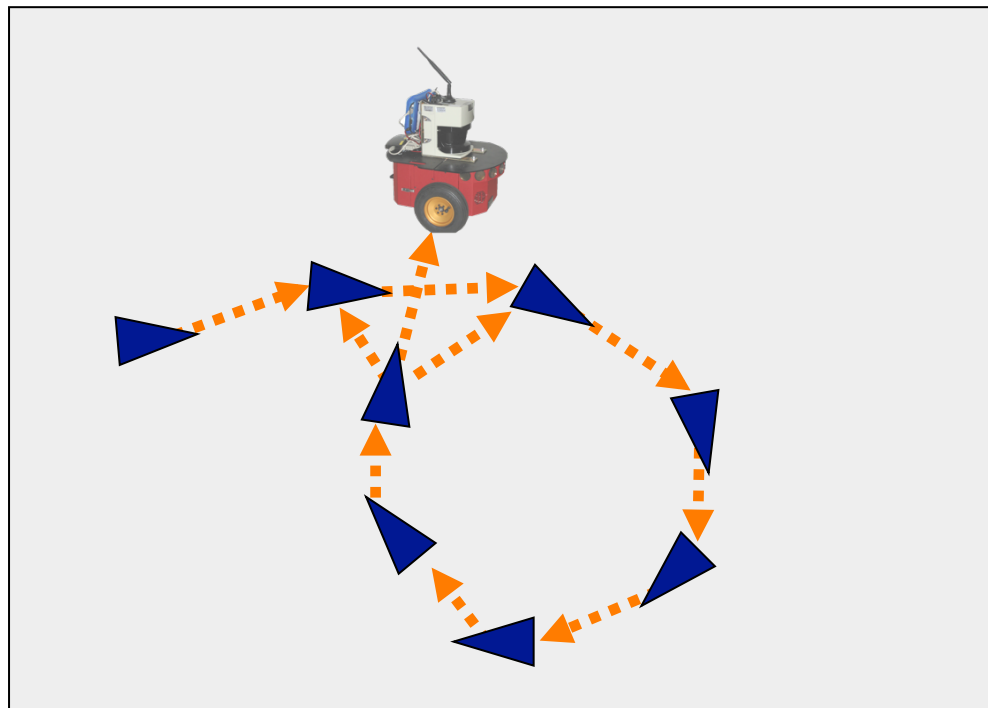


▶ Robot pose

⋯▶ Constraint

# SLAM

- Observing previously seen areas generates constraints between non-successive poses
- **How to obtain the constraints?**

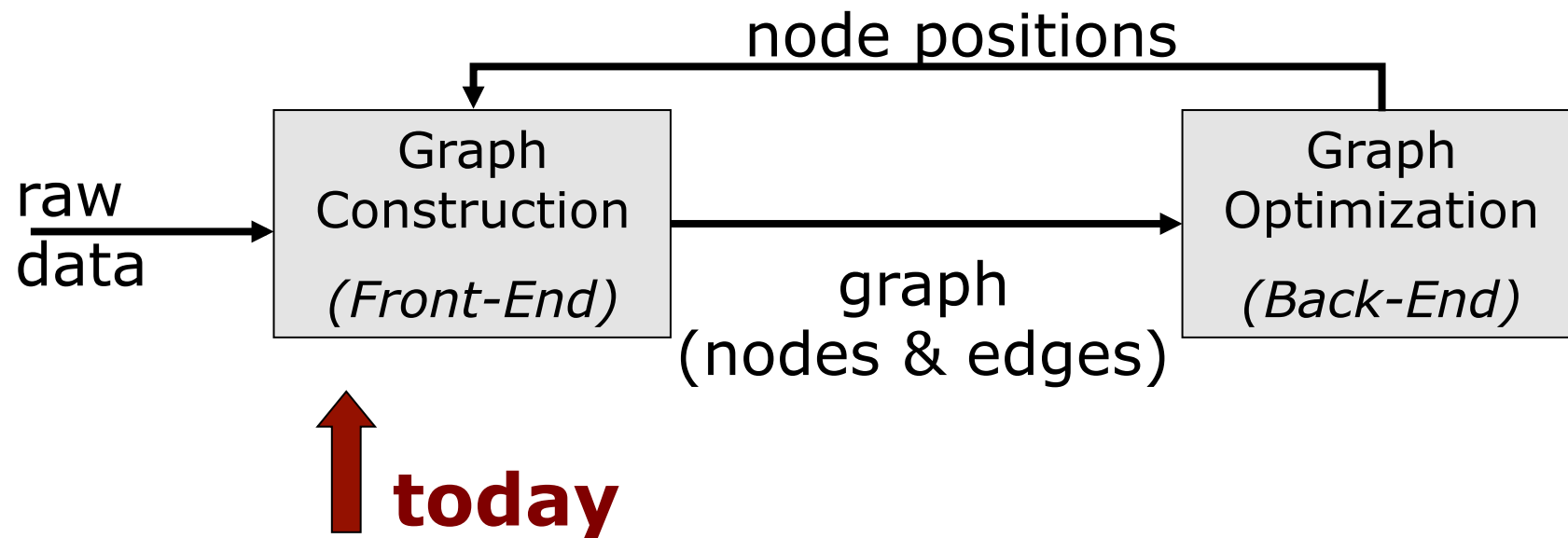


Robot pose



Constraint

# Interplay between Front-End and Back-End



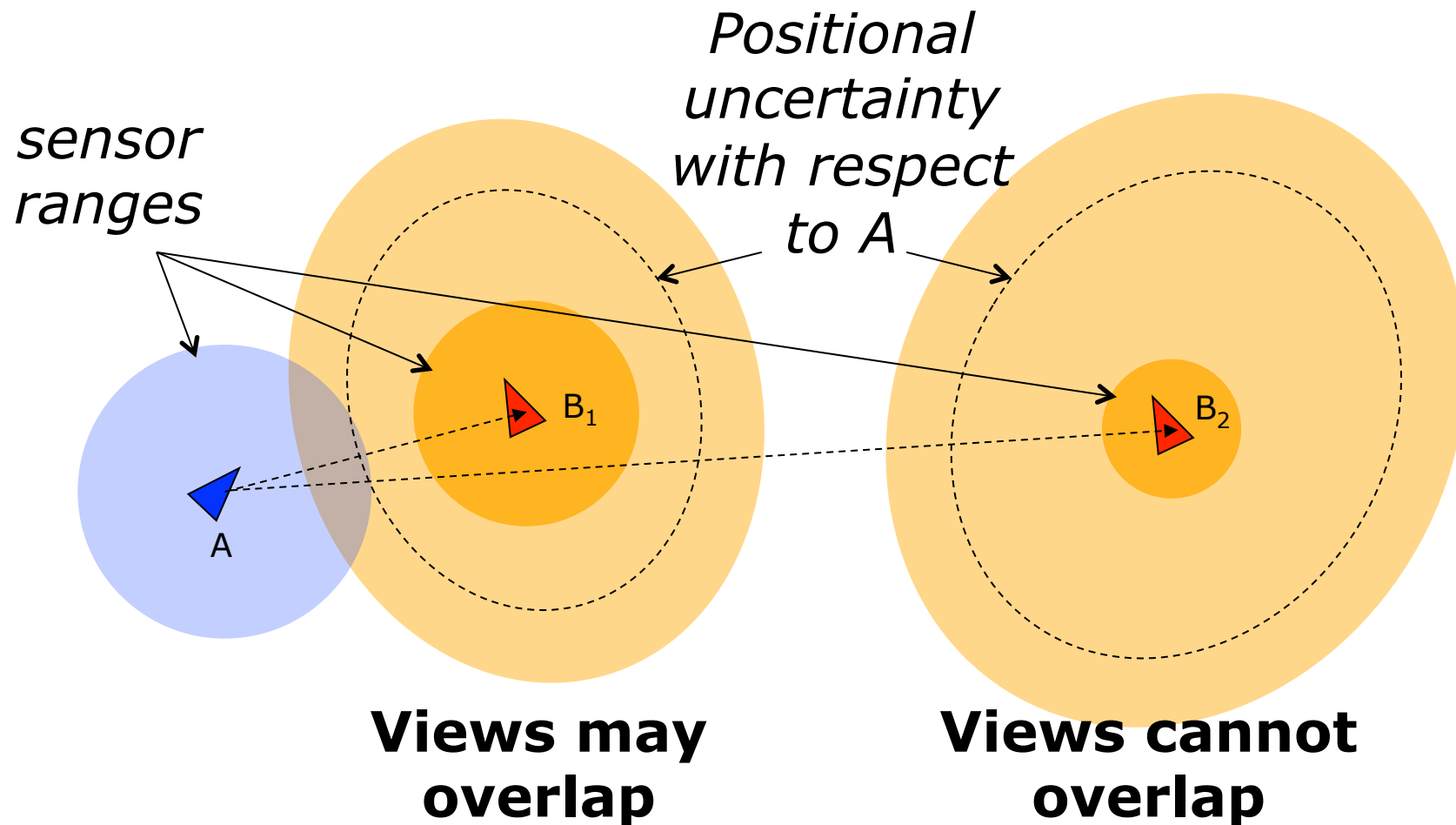


# Constraints From Matching

- Constraints can be obtained from matching observations
  - Scan-matching
  - Feature-based matching
  - Descriptor-based matching

# Where to Search for Matches?

- Consider uncertainty of the nodes with respect to the current one



# Simple ICP-Based Approach

- Estimate uncertainty of nodes relative to the current pose
- Sample poses in relevant area
- Apply ICP – Iterative Closest Point
- Evaluate match
- Accept match based on a threshold

**Problems?**

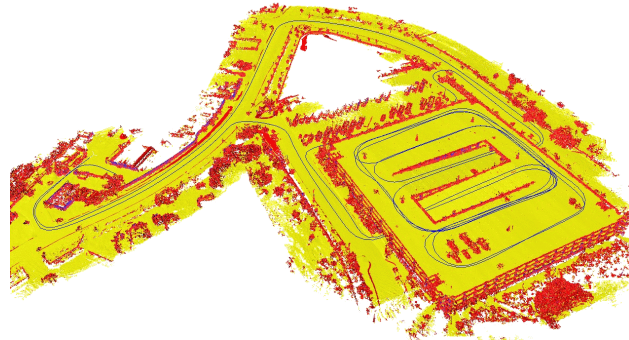
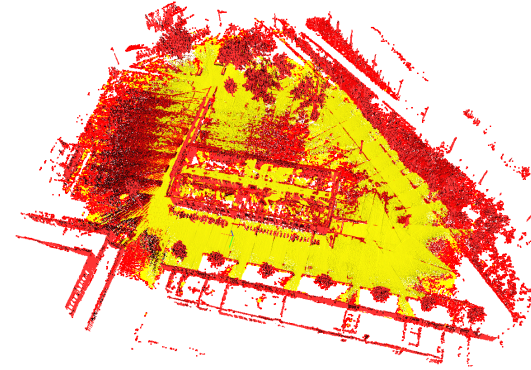
# Problems

- ICP is sensitive to the initial guess
- Inefficient sampling
- Ambiguities in the environment

# Problems

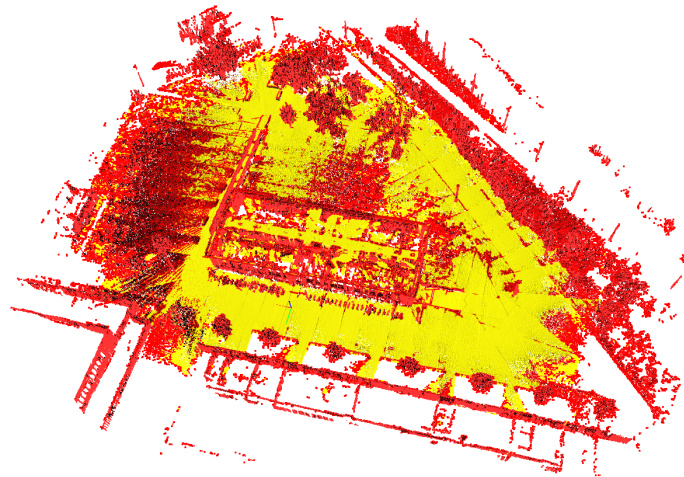
- **ICP is sensitive to the initial guess**
- **Inefficient sampling**
- Ambiguities in the environment

# Examples

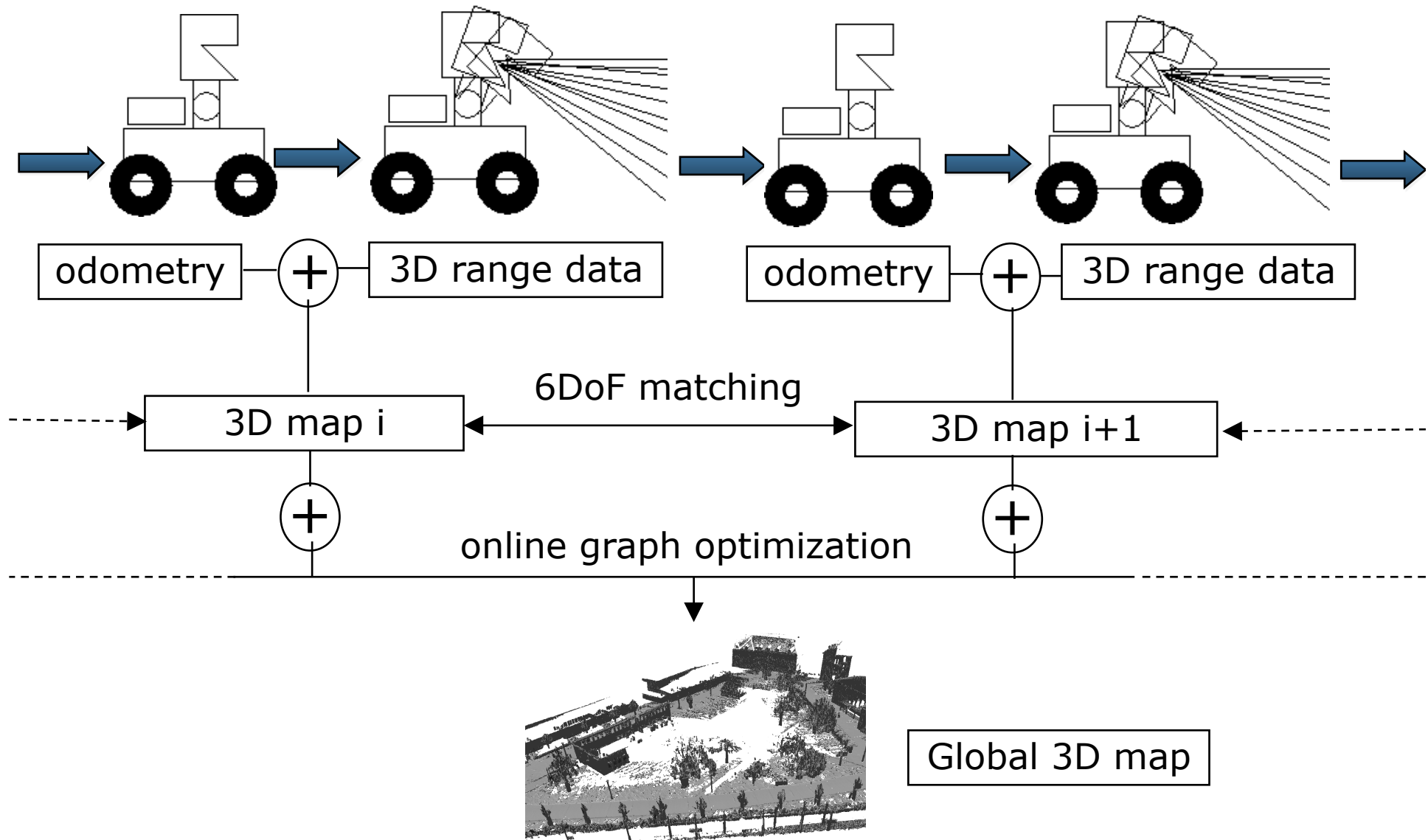


# Learning 3D Maps with Laser Data

- Robot that provides odometry
- Laser range scanner on a pan-tilt-unit

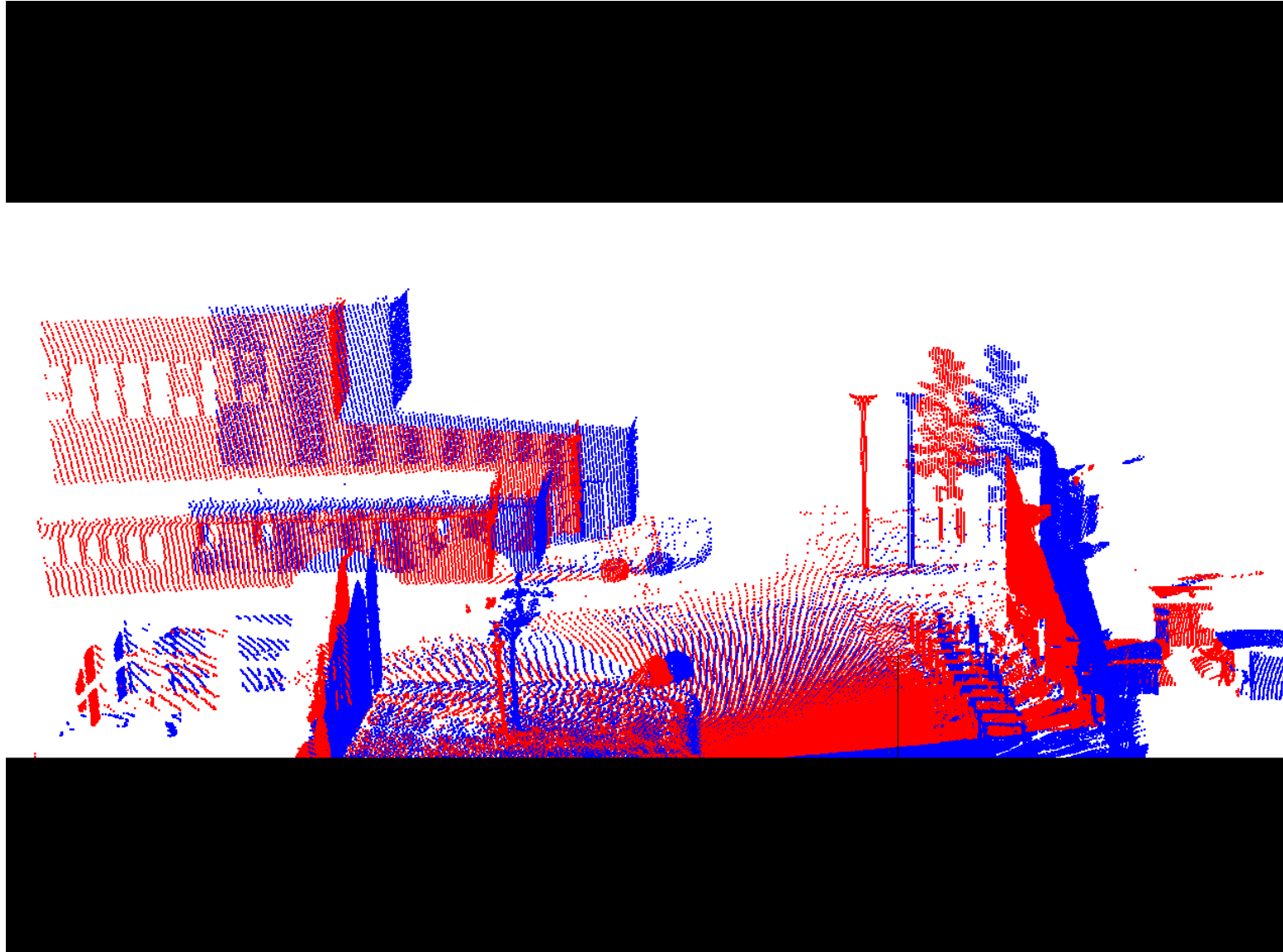


# Incremental 6D SLAM





# Aligning Consecutive Maps



# Aligning Consecutive Maps

- Let  $\mathbf{u}_{i_c}$  and  $\mathbf{u}'_{j_c}$  be corresponding points
- Find the parameters  $R$  and  $t$  which minimize the sum of the squared error

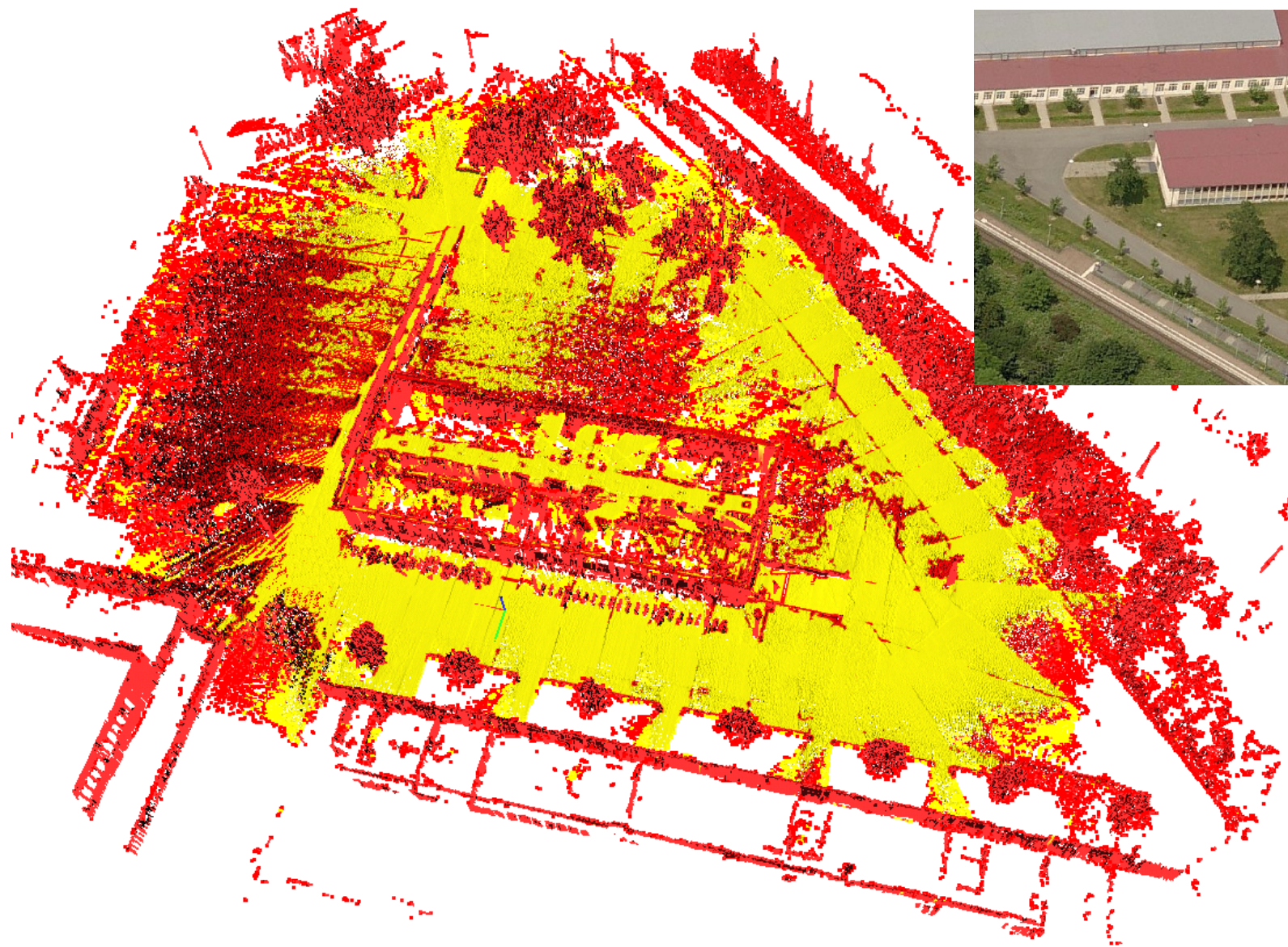
- ICP

$$e(R, t) = \sum_{c=1}^C d(\mathbf{u}_{i_c}, \mathbf{u}'_{j_c})$$

- ICP with additional knowledge

$$e(R, t) = \underbrace{\sum_{c=1}^{C_1} d_v(\mathbf{u}_{i_c}, \mathbf{u}'_{j_c})}_{\text{vertical objects}} + \underbrace{\sum_{c=1}^{C_2} d(\mathbf{v}_{i_c}, \mathbf{v}'_{j_c})}_{\text{traversable}} + \underbrace{\sum_{c=1}^{C_3} d(\mathbf{w}_{i_c}, \mathbf{w}'_{j_c})}_{\text{non-traversable}}$$

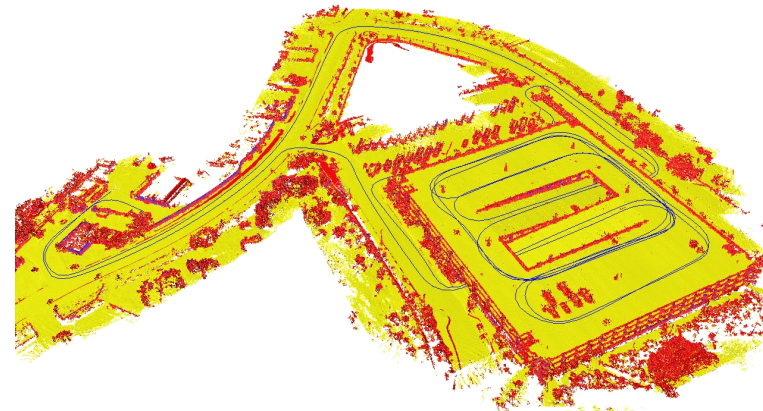
# Online Estimated 3D Map





# Mapping with a Robotic Car

- 3D laser range scanner (Velodyne)
- Use map for autonomous driving

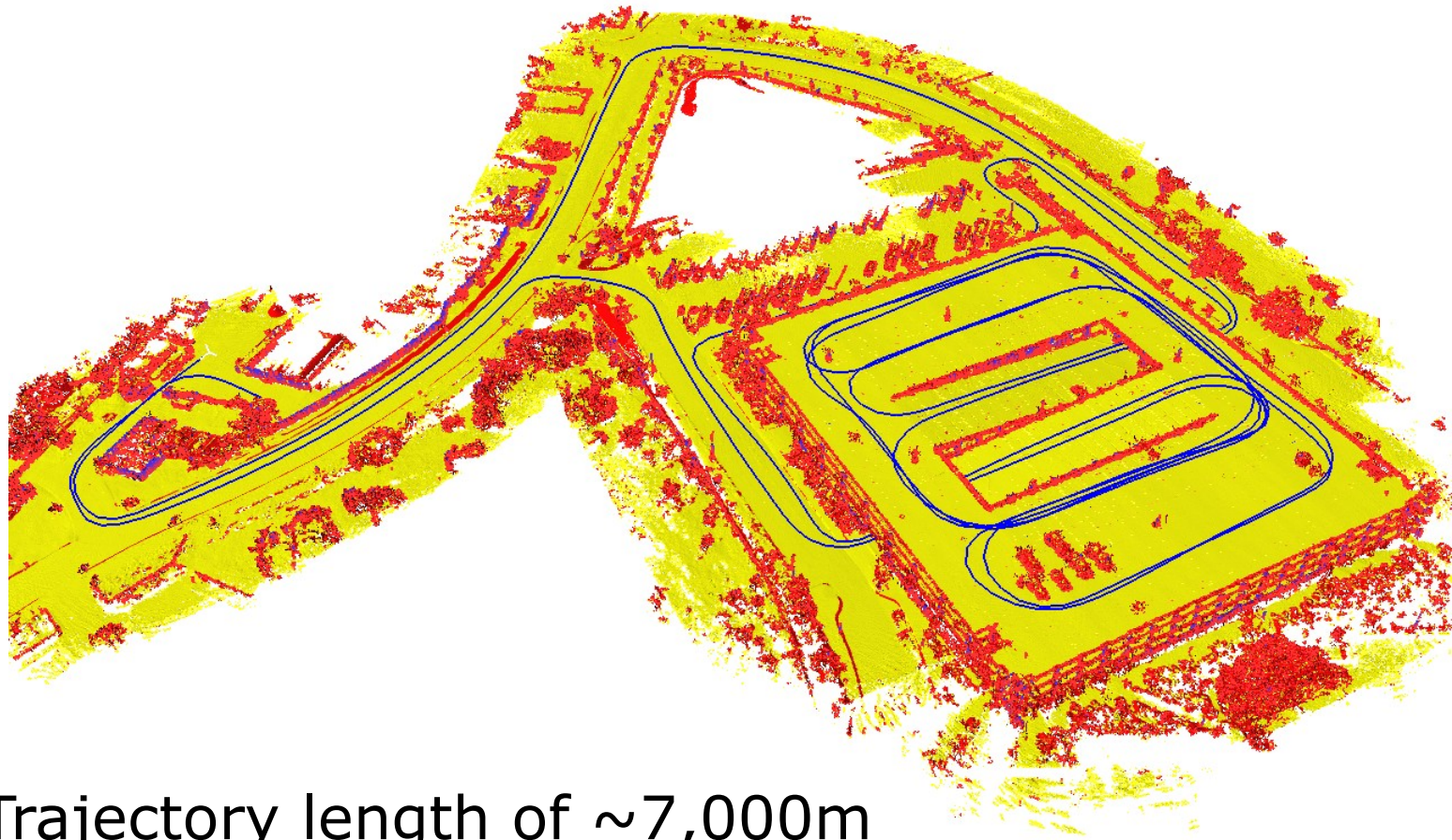


# Parking Garage



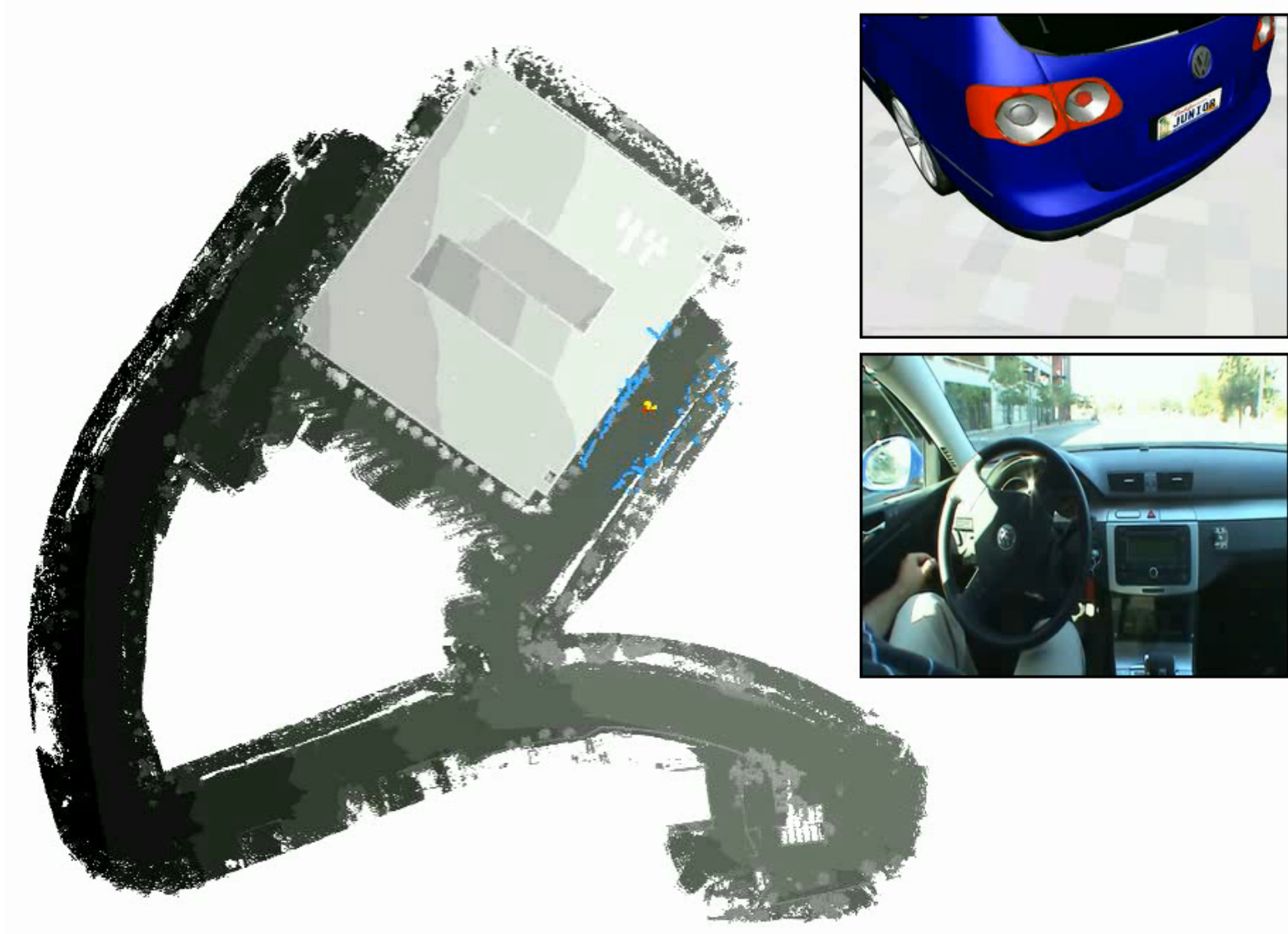


# Resulting Map



- Trajectory length of  $\sim 7,000\text{m}$
- 1661 local 3D maps, cell size of  $20\text{cm} \times 20\text{cm}$

# Map-based Autonomous Parking



# Mapping with Arial Vehicles

- Flying vehicles equipped with cameras and an IMU



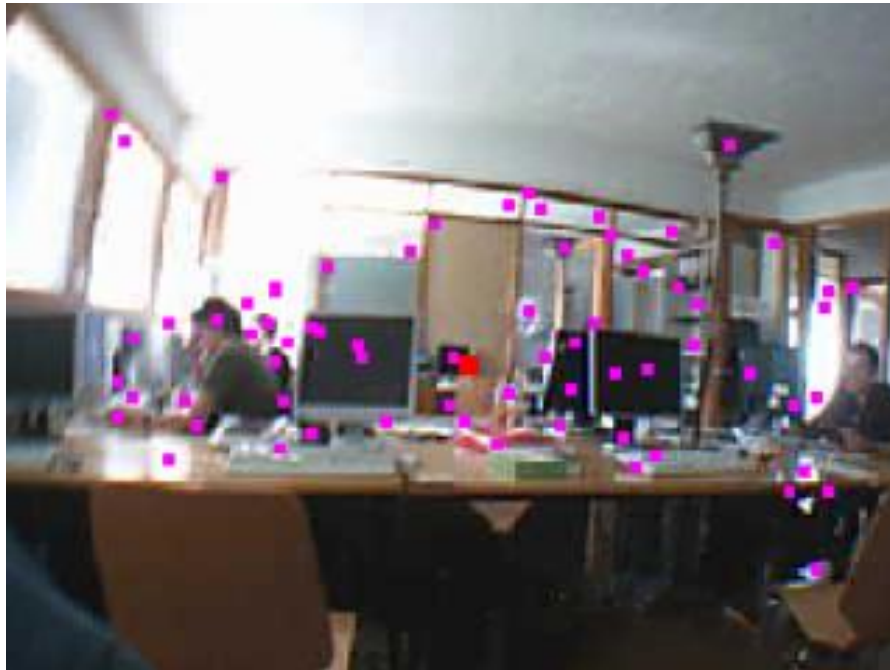


# Examples of Camera Images



# SURF Features

- Provide a description vector and an orientation
- Descriptor is invariant to rotation and scale



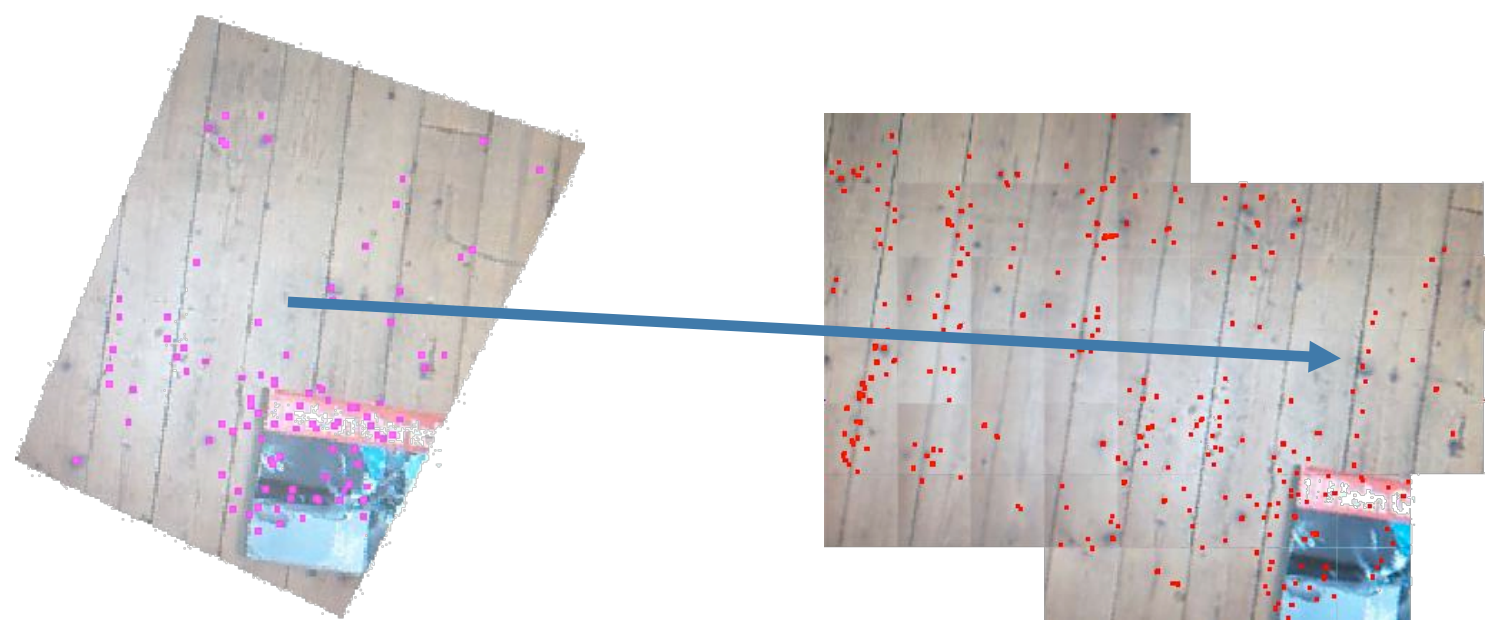
# Determining the Camera Pose

**Wanted:**  $x, y, z, \varphi, \theta, \Psi$  (roll, pitch, yaw)

- IMU determines roll and pitch accurately
- $x, y, z$  and the heading (yaw) have to be calculated based on the camera images

 3D positions of **two** image features is sufficient to determine the camera pose

# Feature Matching for Pose Estimation



features in image

features in map

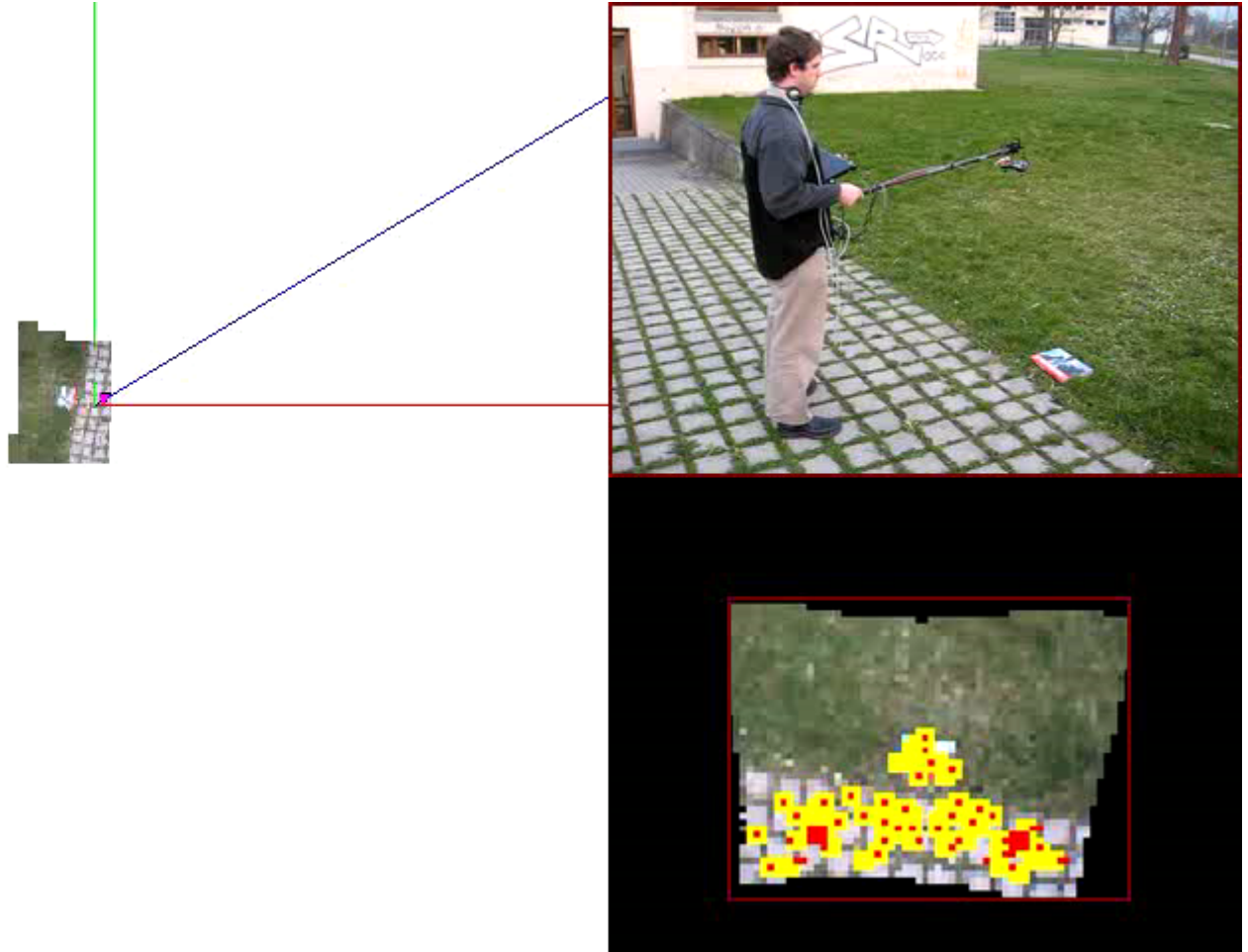
# Camera Pose Estimation

1. Find possible matches (kd-tree)
2. Order matches by descriptor distance
  - Use two matches to calculate the camera position, start with the best one
  - Re-project all features accordingly to get a quality value about this pose
  - Repeat until satisfactory pose is found
3. Update map

# Finding Edges in the Graph

- **Visual odometry:** Match features against the  $N$  previously observed ones
- **Localization:** Match against features in the map in a given region around the odometry estimate (local search)
- **Loop closing:** Match a subset of the features against all map features. Match leads to a localization step

# Outdoor Example



# Resulting Trajectory



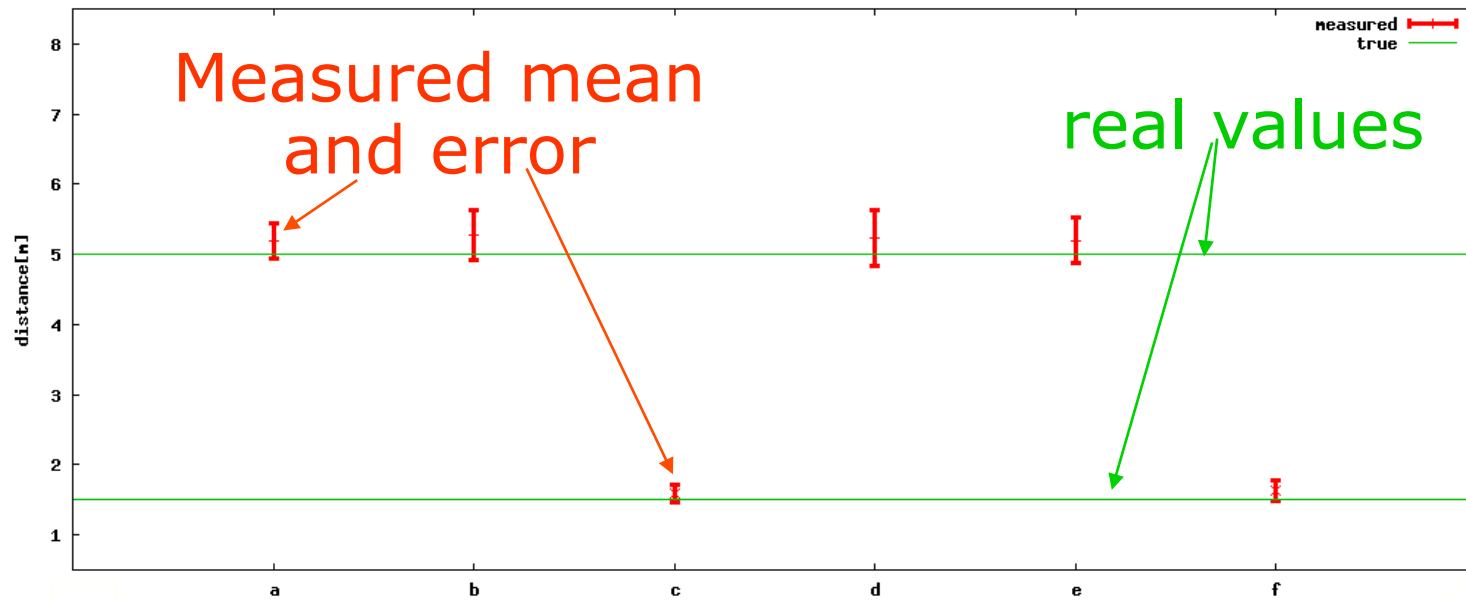
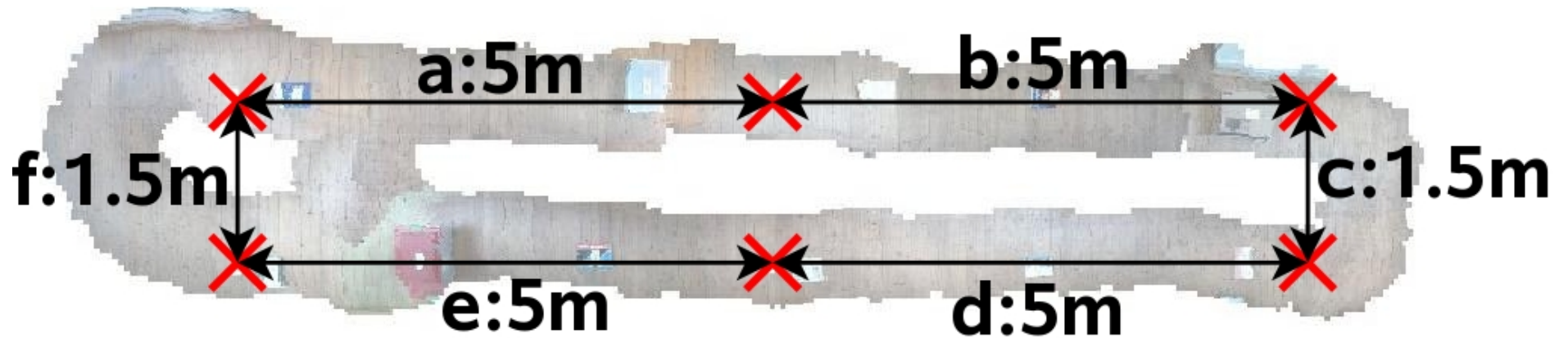
- Length (Google Earth): 188m
- Estimated length: 208m



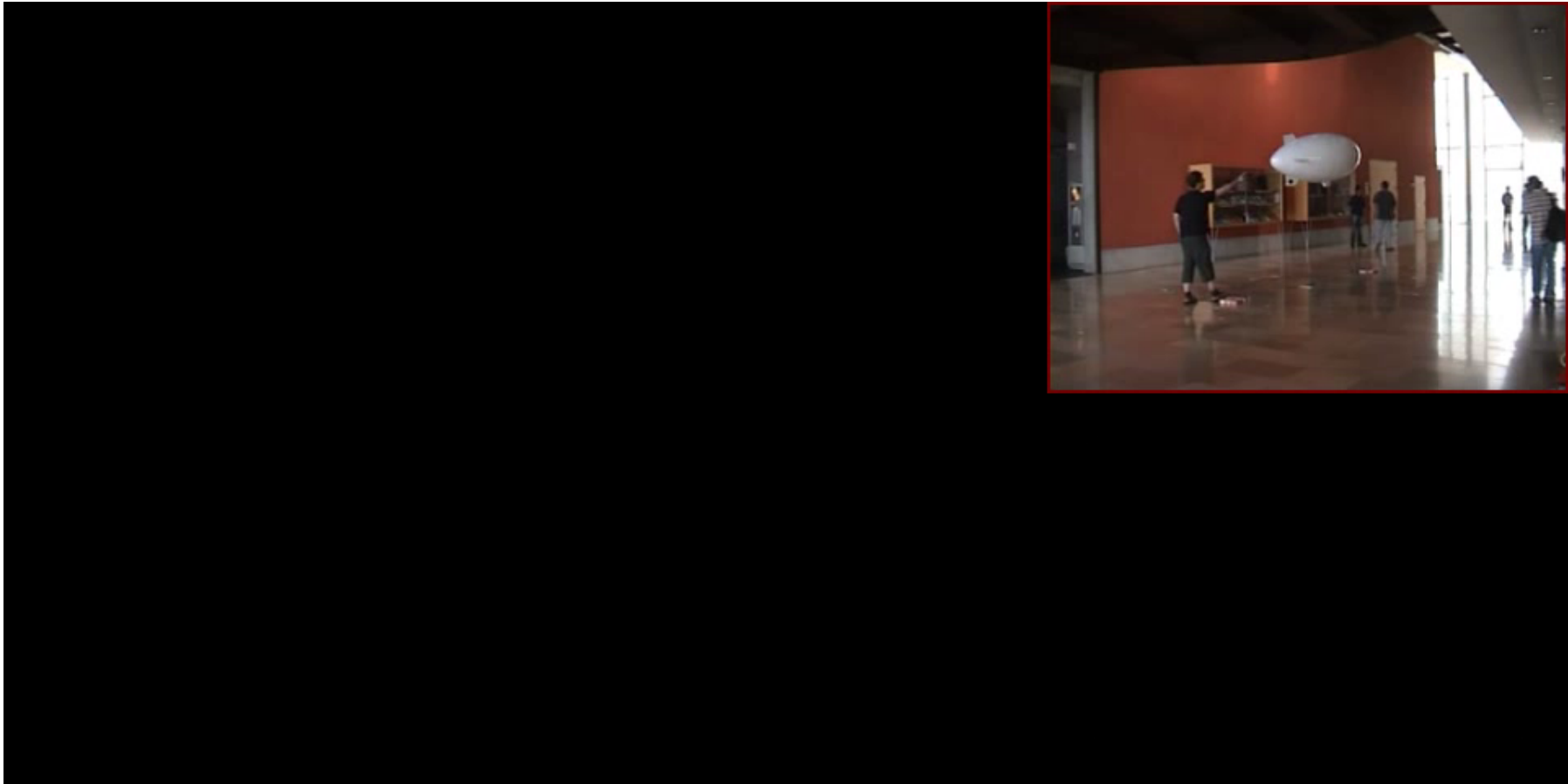
# Indoor Example



# Ground Truth



# System on a Blimp

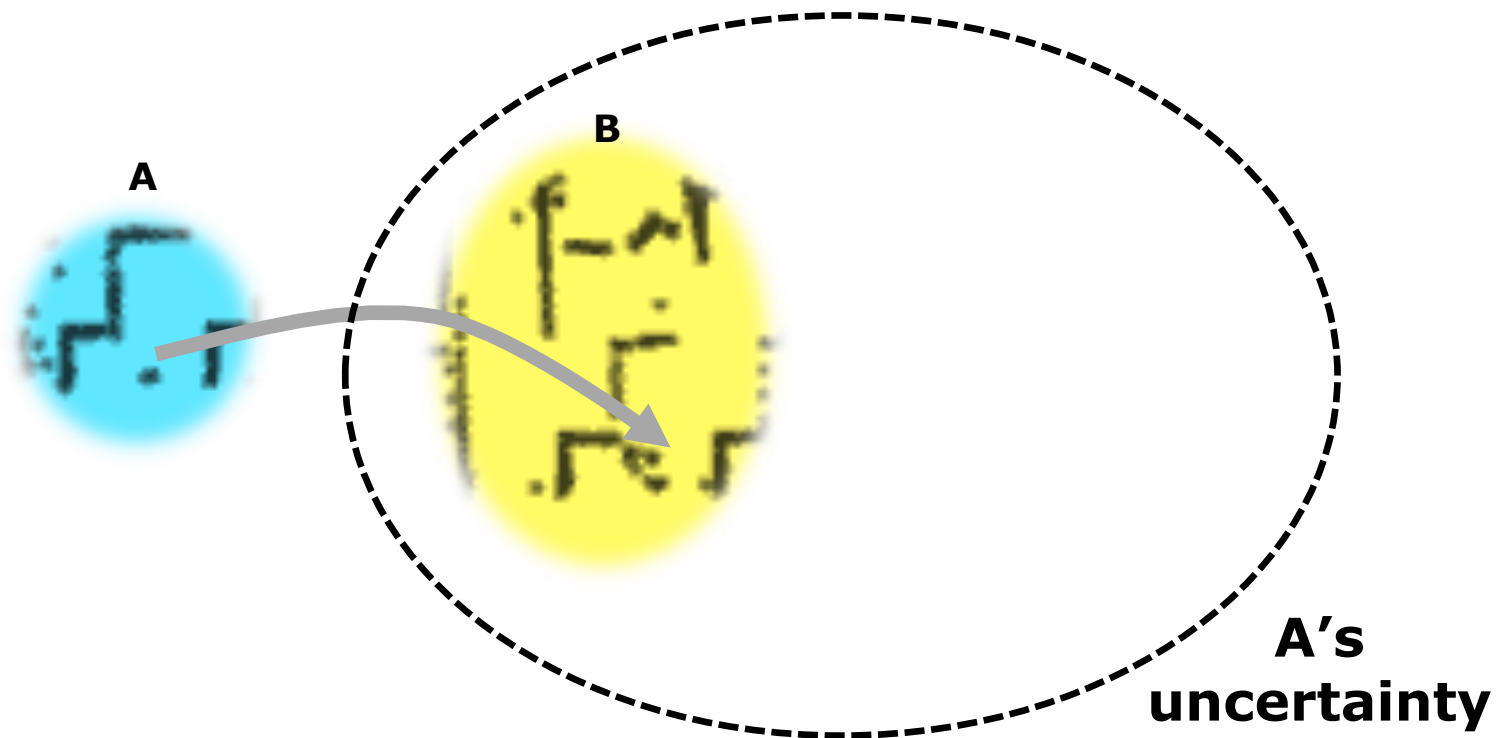


# Problems

- ICP is sensitive to the initial guess
- Inefficient sampling
- **Ambiguities in the environment**
- Dealing with ambiguous areas in an environment is essential for robustly operating robots

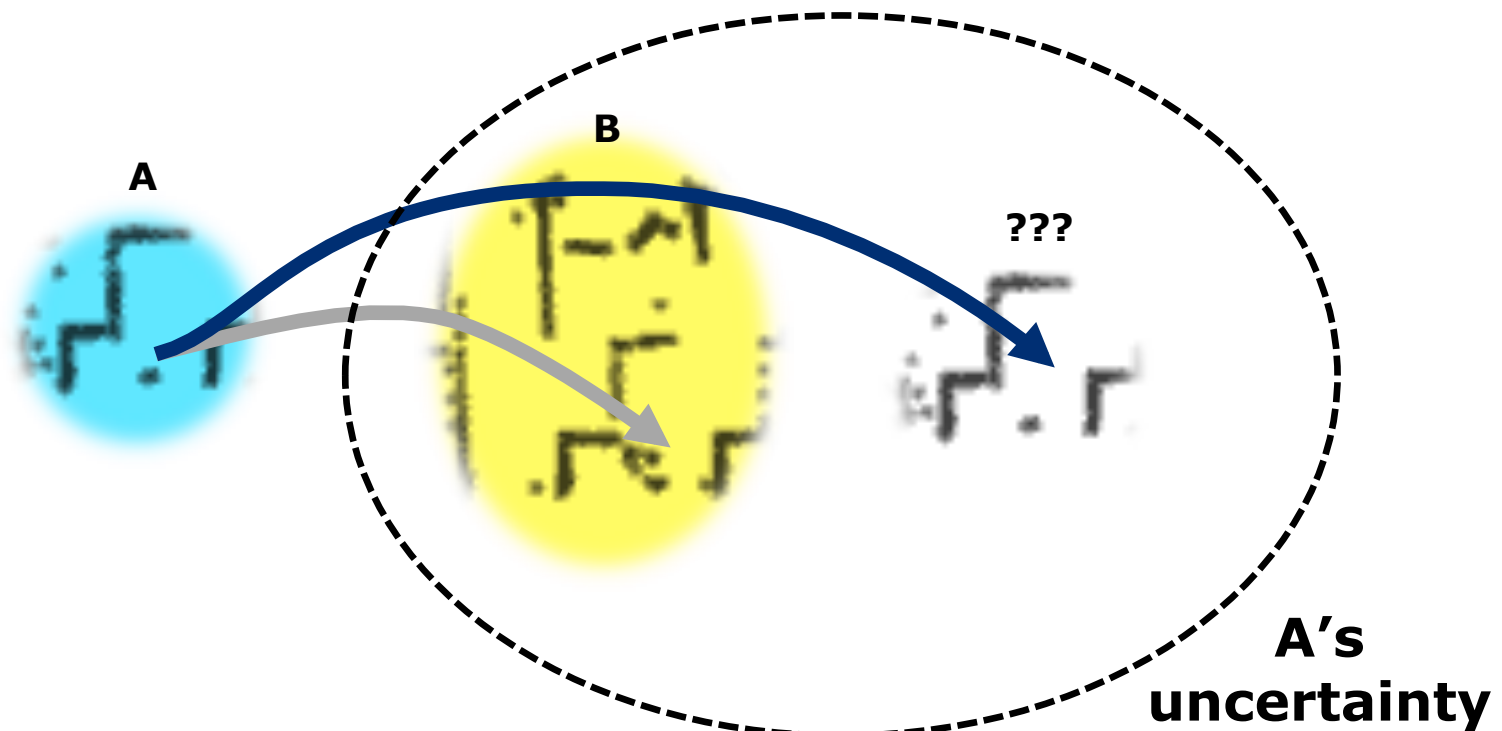
# Ambiguities - Global Ambiguity

- A is inside the uncertainty ellipse
- Are A and B the same place?



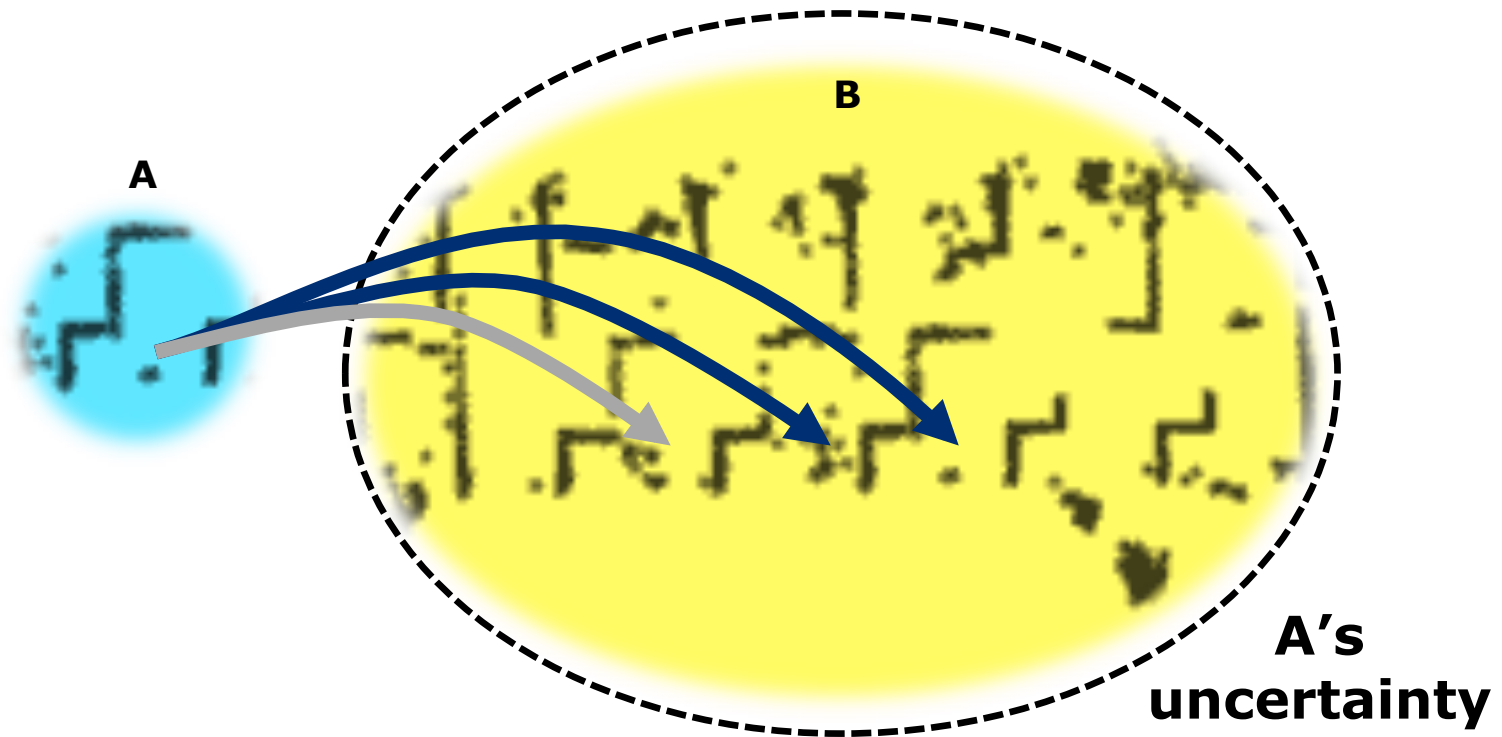
# Ambiguities - Global Ambiguity

- A is inside the uncertainty ellipse
- A and B might not be the same place



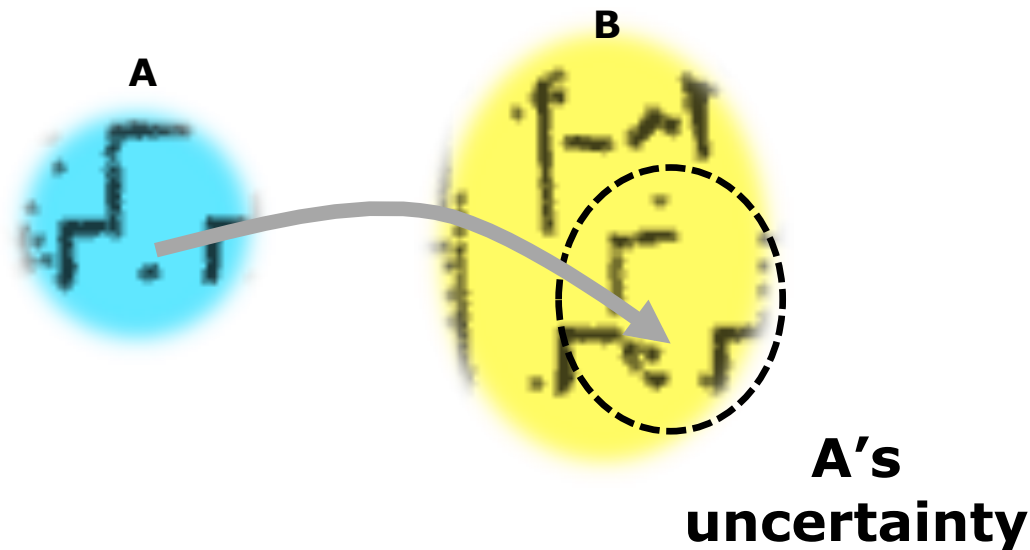
# Ambiguities - Global Ambiguity

- A is inside the uncertainty ellipse
- A and B are not the same place



# Ambiguities - Global Sufficiency

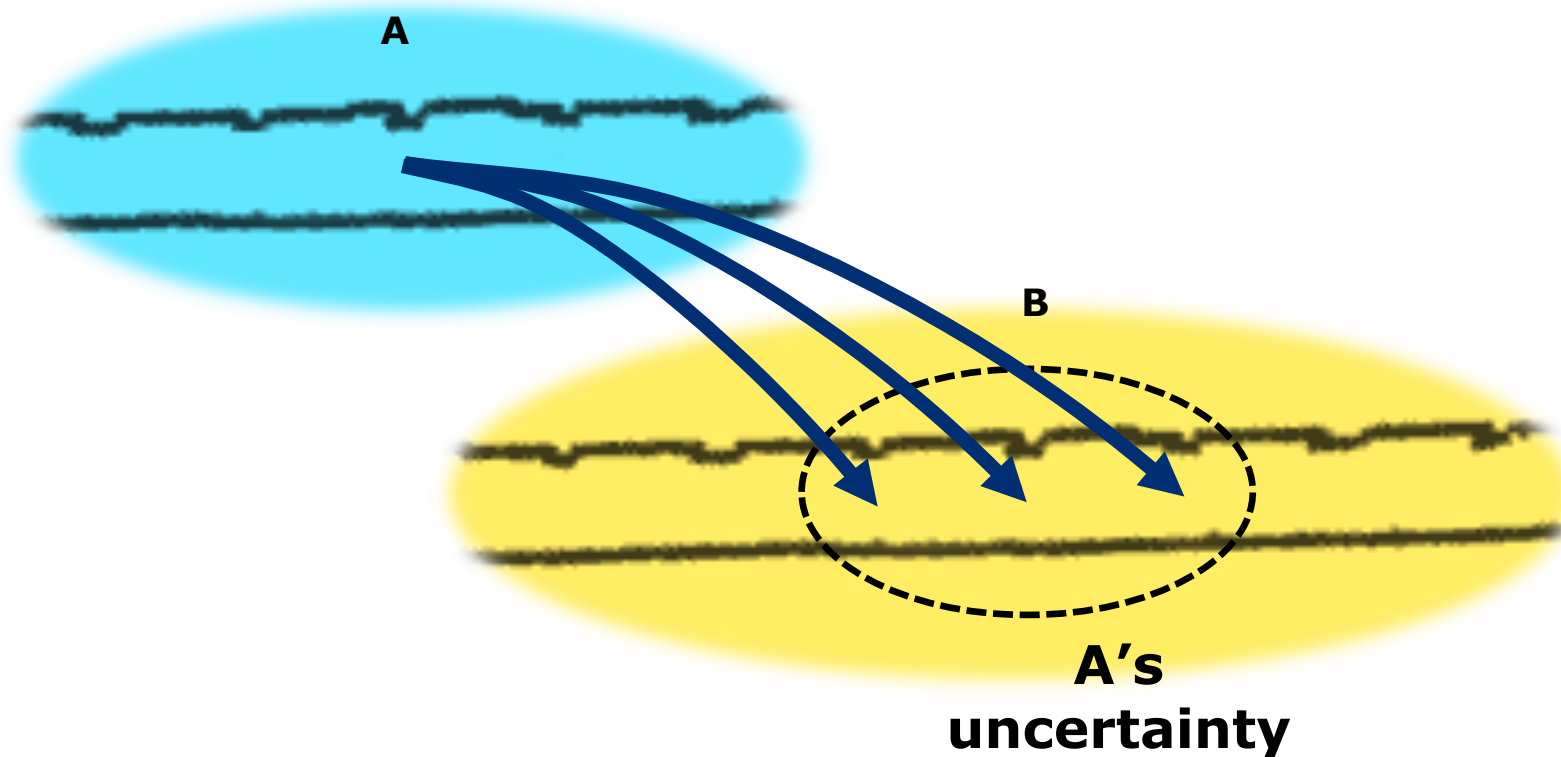
- A is inside the uncertainty ellipse
- There is no other possibility for a match





# Ambiguities - Local Ambiguity

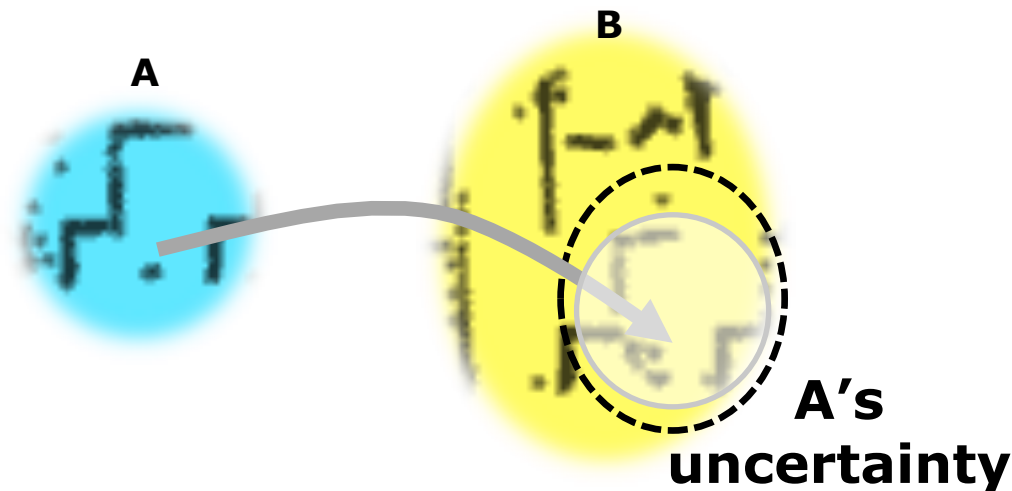
- “Picket Fence Problem”: largely overlapping local matches



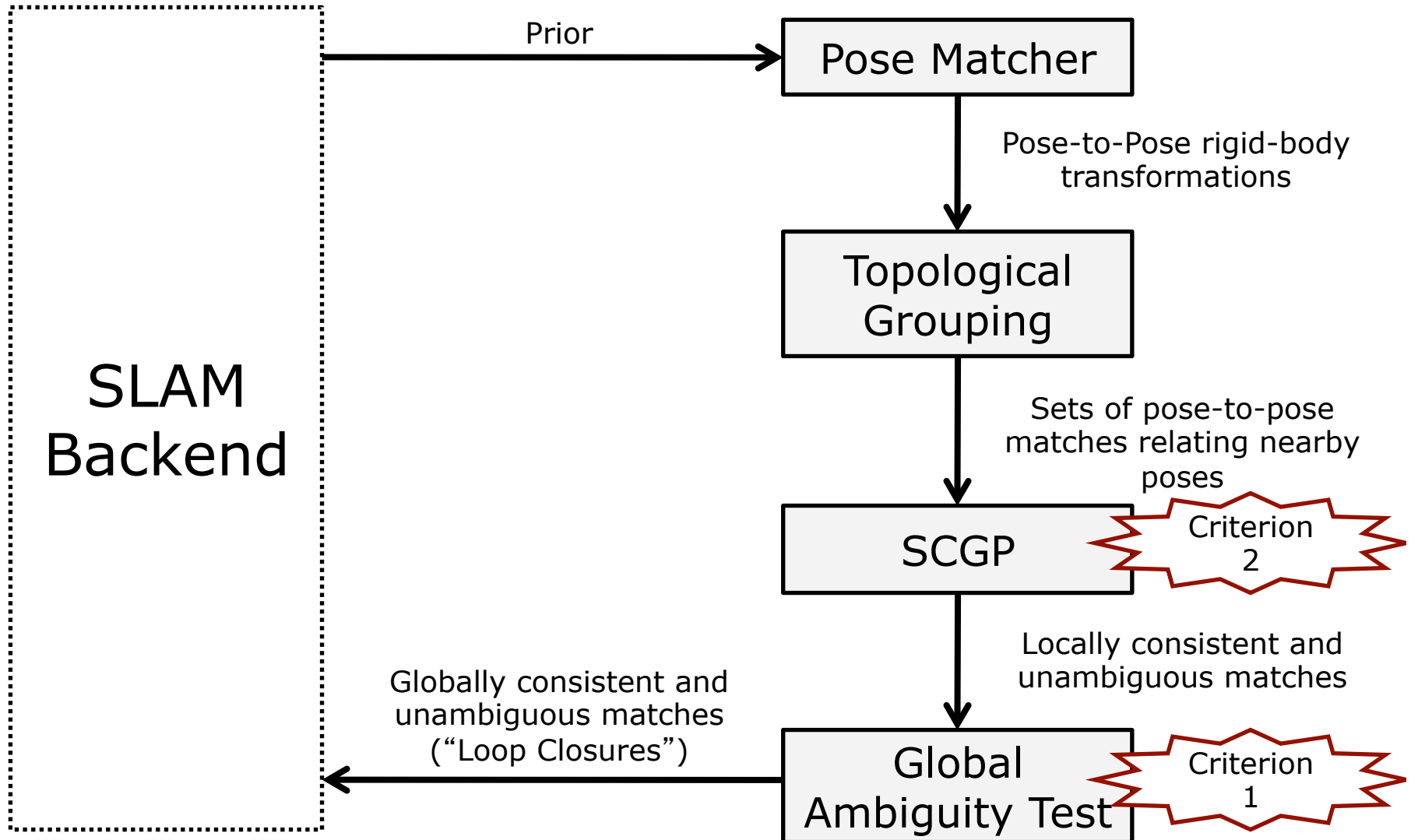
# Global Match Criteria

1. Global Sufficiency: There is no disjoint match (“A is not somewhere else entirely”)
2. Local unambiguity: There are no overlapping matches (“A is either here or somewhere else entirely”)

**Both need to be satisfied for a match**

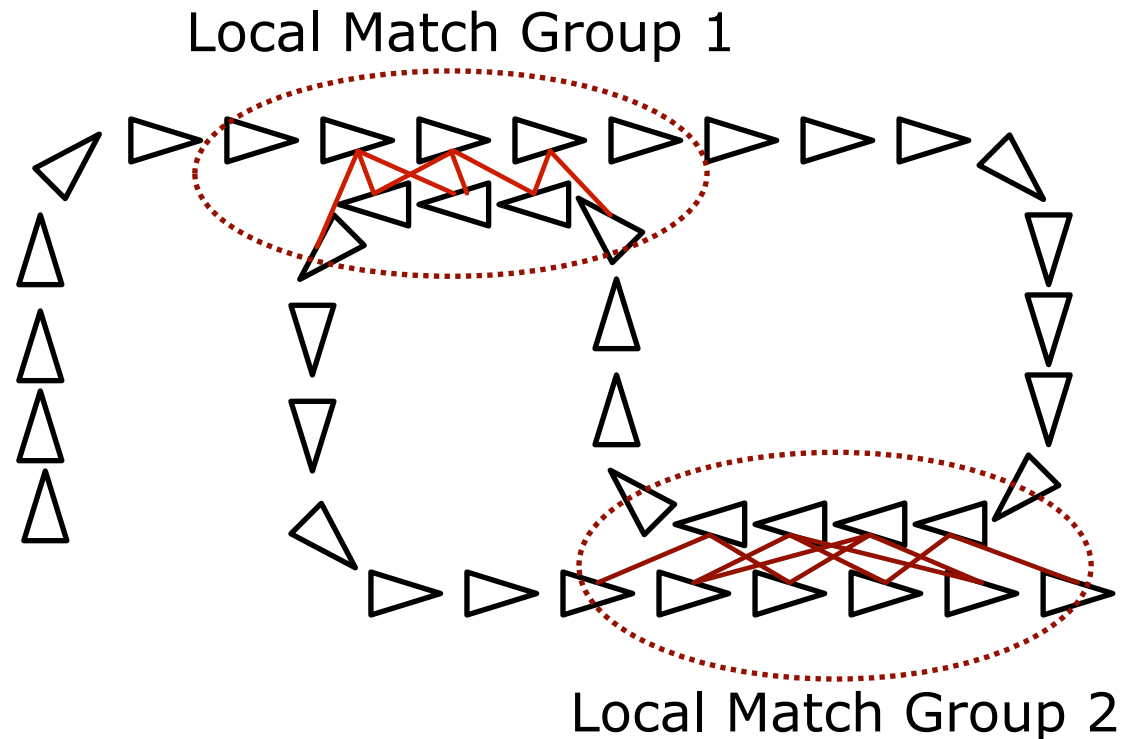


# Olson's Proposal



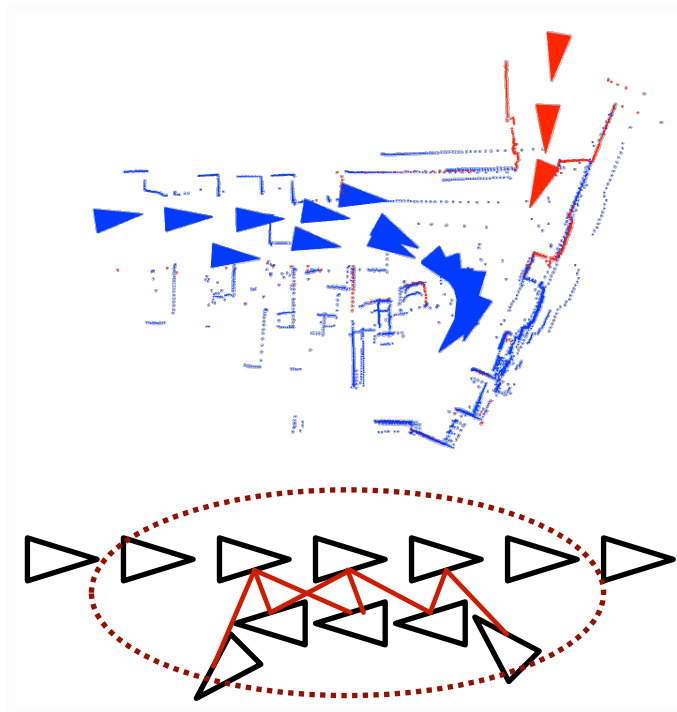
# Topological Grouping

- Group together topologically-related pose-to-pose matches to form local matches
- Each group asks a “topological” question: Do two local maps match?

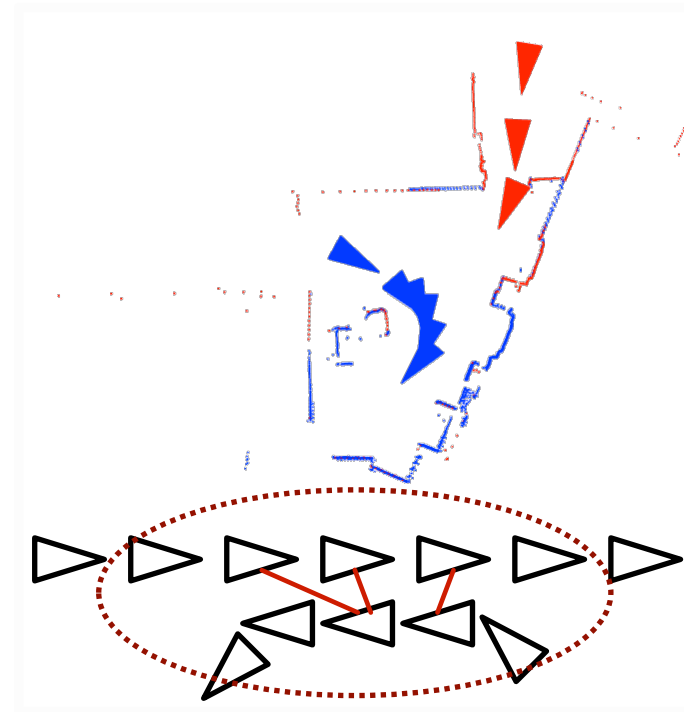
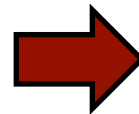


# Local Unambiguous Matches

- Goal



Unfiltered Local Match  
(set of pose-to-pose matches)



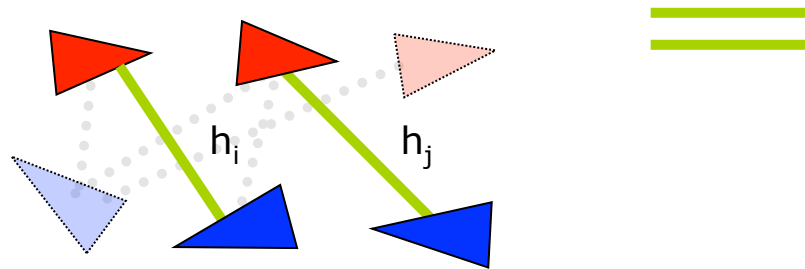
Locally consistent and  
unambiguous local match  
(set of pose-to-pose matches)

# Locally-Consistent Matches

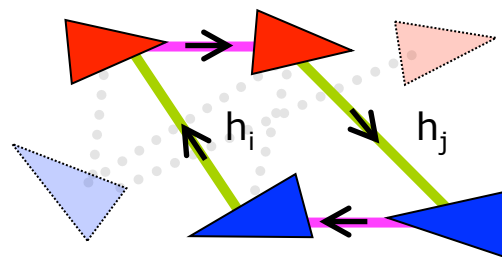
- Correct pose-to-pose hypotheses must agree with each other
- Incorrect pose-to-pose hypotheses tend to disagree with each other
- Find subset of self-consistent of hypotheses
- Multiple self-consistent subsets, are an indicator for a “picket fence”!

# Do Two Hypotheses Agree?

- Consider two hypotheses  $i$  and  $j$  in the set:



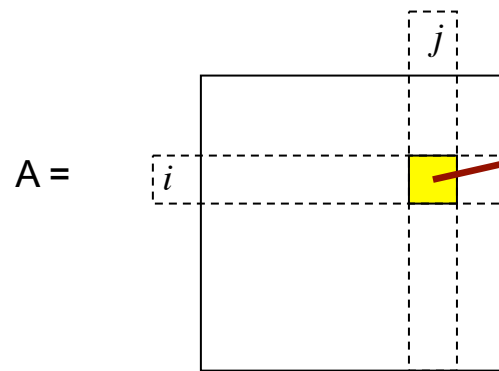
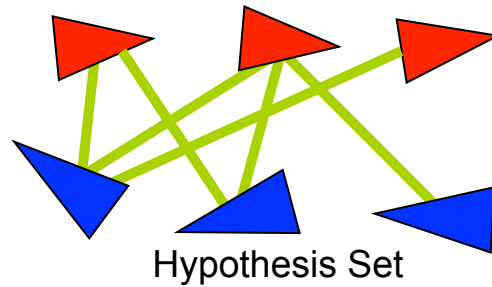
- Form a loop using edges from our prior



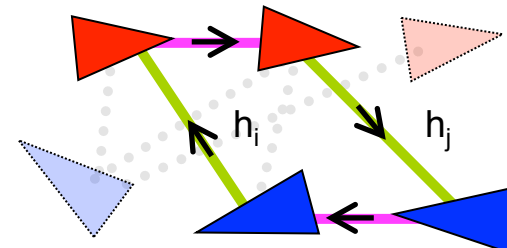
**Rigid-body transformation around the loop should be the identity matrix**

# Idea of Olson's Method

- Form pair-wise consistency matrix **A**



$$A_{ij} = P(\text{loop}(i, j) = I \mid h_i, h_j)$$

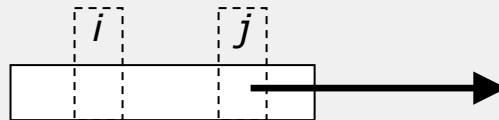




# Single Cluster Graph Partitioning

- Idea: Identify the subset of consistent hypothesis
- Find the best **indicator vector** (represents a subset of the hypotheses)

Indicator vector  $v$



$$v_i = \begin{cases} 1 & \text{if } h_i \text{ is correct,} \\ 0 & \text{if } h_i \text{ is incorrect} \end{cases}$$

# Single Cluster Graph Partitioning

- Identify the subset of hypotheses that is maximally self-consistent
- Which subset  $\mathbf{v}$  has the **greatest average pair-wise consistency**  $\lambda$ ?

$$\lambda = \frac{\mathbf{v}^T \mathbf{A} \mathbf{v}}{\mathbf{v}^T \mathbf{v}}$$

Sum of all pair-wise consistencies between hypotheses in  $\mathbf{v}$

Number of hypotheses in  $\mathbf{v}$

- Densest Subgraph Problem *Gallo et al 1989*

# Consistent Local Matches

- We want find  $\mathbf{v}$  that maximizes  $\lambda(\mathbf{v})$

$$\lambda(\mathbf{v}) = \frac{\mathbf{v}^T \mathbf{A} \mathbf{v}}{\mathbf{v}^T \mathbf{v}}$$

- Treat as continuous problem
- Derive and set to zero

$$\frac{\partial \lambda(\mathbf{v})}{\partial \mathbf{v}} = 0$$

- Which leads to (for symmetric A)

$$\mathbf{A} \mathbf{v} = \lambda \mathbf{v}$$

# Consistent Local Matches

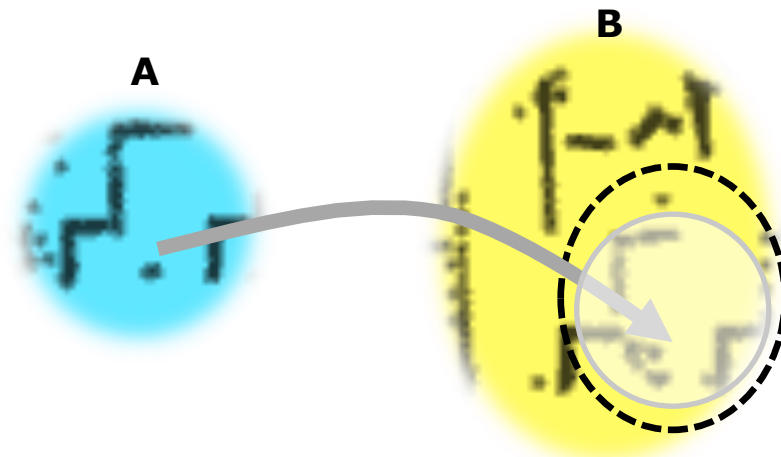
- $A\mathbf{v} = \lambda\mathbf{v}$  : Eigenvalue/vector problem
- The dominant eigenvector  $\mathbf{v}_1$  maximize

$$\lambda(\mathbf{v}) = \frac{\mathbf{v}^T \mathbf{A} \mathbf{v}}{\mathbf{v}^T \mathbf{v}}$$

- The hypothesis represented by  $\mathbf{v}_1$  is maximally self-consistent subset
- If  $\lambda_1/\lambda_2$  is large ( $>2$ ) then  $\mathbf{v}_1$  is locally unambiguous
- Discretize  $\mathbf{v}_1$  after maximization

# Global Consistency

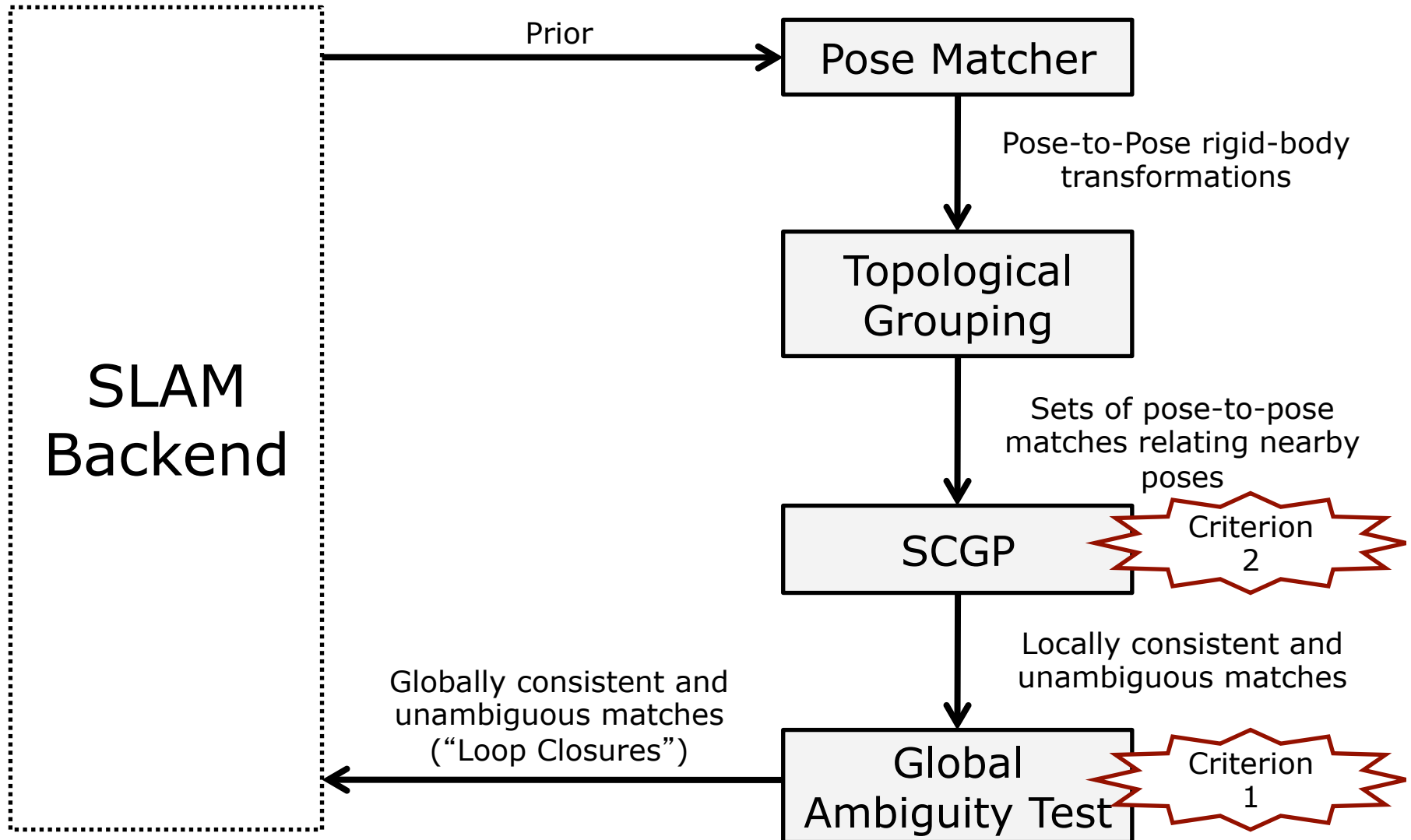
- **Correct method:** can two copies of A be arranged so that they both fit inside the covariance ellipse?
- **Approximation:** is the dimension of A at least half the length of the dominant axis of the covariance ellipse?
- Potential failures for narrow local matches



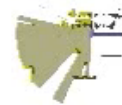
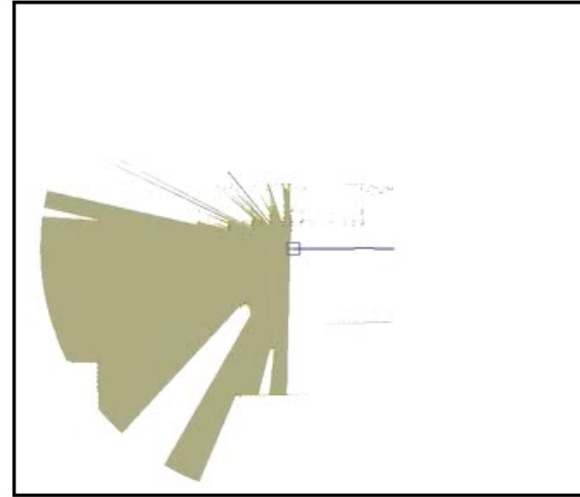
## Note on the Uncertainty

- In graph-based SLAM, computing the uncertainty relative to  $A$  requires inverting the Hessian  $\mathbf{H}$
- Fast approximation by Dijkstra expansion (“propagate uncertainty along the shortest path in the graph”)
- Conservative estimate

# Olson's Proposal



# Example





# Conclusions

- Local matching can be used to establish global matches
- Matching observations is used to generate pose-to-pose hypotheses (constraints)
- Local matches assembled from pose-to-pose hypotheses
- Local ambiguity (“picket fence”) can be resolved via SCGP’s confidence metric
- Positional uncertainty: more uncertainty requires more evidence