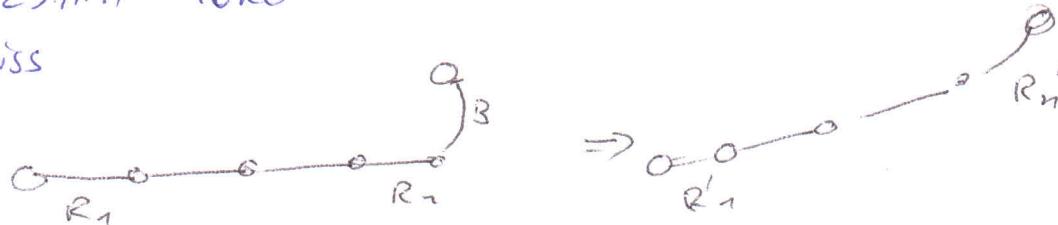


Cyrill Stachniss



$$R_1 \dots R_n B = R_1' \dots R_n' ; R_k \text{ relative rotations}$$

\Rightarrow Goal: Find $R_1' \dots R_n'$

* let the first node be the Ref. frame

* we want one rotation axis for the correction

$$\Rightarrow A_n' = A_n B = Q A_n \quad \text{with } A_n \text{ being the rotation in the } \underline{\text{global frame}}$$

\downarrow

$$\begin{matrix} A_n' \\ " \\ R_n' \end{matrix} = \begin{matrix} A_n \\ " \\ R_n \end{matrix} B$$

$$Q = Q_1 \dots Q_n$$

$$Q_n = \text{slerp}(Q, u_{k-1})^T \text{slerp}(Q, u_k) \quad u_k \in [0, 1]$$

$$\begin{aligned}
 R_k' &= [A_{k-1}']^T A_k' & A_k' &= Q_1 \dots Q_k A_k \\
 &= [Q_{1:k-1} \ A_{k-1}]^T A_k' \\
 &= A_{k-1}^T Q_{k-1}^T \dots Q_1^T A_k'^\dagger \\
 &= A_{k-1}^T Q_{k-1} \dots Q_1^T [Q_1 \dots Q_k \ A_k] \\
 &= A_{k-1}^T Q_k A_k \\
 &= (R_{1:k-1})^T Q_k R_{1:k}
 \end{aligned}$$