Albert-Ludwigs-Universität Freiburg
Institut für Informatik
Lecture: Introduction to Mobile Robotics
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Sheet 8

Topic: Mapping with Known Poses

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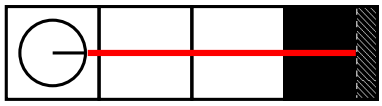
Exercise 1: Counting Model

A robot applies the so-called simple counting approach to build a grid map of a 1D environment consisting of the cells $c_0, \ldots, c_3$. While standing in cell c_0, the robot integrates four measurements $z_{t_0}, \ldots, z_{t_3}$. After integrating these measurements, the resulting belief of the robot with regards to the occupancy of the four cells is $b_0 = 0,\ b_1 = \frac{1}{4},\ b_2 = \frac{2}{3},\ b_3 = 1$. Given that the first three measurements are $z_{t_0} = 1,\ z_{t_1} = 2,\ z_{t_2} = 3$, compute the value of the last measurement z_{t_3}.

Exercise 2: Occupancy Mapping

A robot has to build an occupancy grid map (cells $c_0, \ldots c_n$) of a simple one-dimensional environment using a sequence of measurements from a range sensor.



Assume a very simple sensor model: every grid cell with a distance (based on its coordinate) smaller than the measured distance is assumed to be occupied with $p = 0.3$. Every cell behind the measured distance is occupied with $p = 0.6$. Every cell located more than $20cm$ behind the measured distance should not be updated. Calculate the resulting occupancy grid map using the inverse sensor model (see mapping lecture PDF, slide 10).

Use Python. Use one array `m=0.5*numpy.ones(21)` for the belief values, and one array which spans from 0 to 200 (both endpoints included) with increments of 10 for the cell coordinates. You can use the following custom range function to include endpoints using Python's in built range function.

```
range_cl = lambda start, end:  range(start, end+1,10)
c = range_cl(0,200)
```

Use `matplotlib.pyplot.plot(c,m)` to visualize the belief.

grid resolution	$10cm$
map length (1d only!)	$2m$
robot's position	c_0
orientation (of the sensor)	heading to c_n (see figure)
measurements (in cm)	$101, 82, 91, 112, 99, 151, 96, 85, 99, 105$
prior	0.5

Exercise 3: Occupancy Mapping

Prove that in the occupancy grid mapping framework the occupancy value of a grid cell $P(m_j|x_{1:t}; z_{1:t})$ is independent of the order in which the measurements are integrated.