

Theoretical Computer Science (Bridging Course)

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Exercise Sheet 6

Due: 11th December 2014

Exercise 6.1 (Turing Machines)

- (a) Design a Turing Machine that decides the language $L := \{0^n 1^n \mid n \geq 1\}$. Explain your choice.
- (b) Give the sequence of configurations for the input string 0011.
- (c) Give the sequence of configurations for the input string 0010.

Exercise 6.2 (Turing Machines)

Describe a TM that decides the language

$$L = \{w \in \{0, 1\}^* \mid |w|_0 = |w|_1\}.$$

where $|w|_0$ and $|w|_1$ are respectively the number of 0's and 1's in w .

Exercise 6.3 (Pushdown Automata, Turing Machines)

How would one simulate a PDA on a Turing machine? Please do not write the Turing machine itself, but rather write the key idea in plain English.

Exercise 6.4 (Non Deterministic Turing Machines)

We call a natural number *composite* if it is not prime¹, formally, the set of natural composite numbers is

$$\{hk \mid h, k \in \mathbb{N}, h, k \geq 2\}$$

Give a nondeterministic Turing machine of the alphabet of vertical bars $\Sigma = \{| \}$ that recognizes the language of composite numbers encoded as unary numbers (i.e. a natural number n is encoded in the form $|^n$). You should not give a formal construction, but describe the idea behind it as precise as possible.

¹Remember that 1 and -1 are not prime numbers! By definition, prime numbers must not be invertible in \mathbb{Z} .